Theoretical Exam
Solutions
For marking:

| Student name: |  |  |  |  |  |  |  |
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| code: |  |  |  |  |  |  |  |
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## References

- https://www.sciencedirect.com/science/article/pii/B9780124186880000010
- https://www.sciencedirect.com/science/article/abs/pii/S0304386X16307095
a) $\rho=\frac{M Z}{N_{A} a^{3}} \Rightarrow M=\frac{\rho N_{A} a^{3}}{Z}=1479.06 \mathrm{~g} \mathrm{~mol}^{-1}$ (1 point)

Tennantite $=\mathrm{Cu}_{\mathrm{a}} \mathbf{X}_{\mathrm{b}} \mathbf{Y}_{\mathrm{c}}$, hence $a=\frac{1479.06 \times 0.5165}{63.55}=12$
$M\left(\mathbf{X}_{\mathrm{b}}\right)=1479.06 \times 0.2026=299.66 \mathrm{~g} \mathrm{~mol}^{-1}$

| $b$ | $M(\mathbf{X}) / \mathrm{g} \mathrm{mol}^{-1}$ |
| :---: | :---: |
| 1 | 299.66 |
| 2 | 149.83 |
| 3 | 99.89 |
| 4 | $74.91(\mathrm{As})$ |
| 5 | 59.93 |
| 6 | 49.94 |
| 7 | 42.81 |
| 8 | 37.46 |

Hence, the only sensible possibility is $b=4$, meaning that $\mathbf{X}=$ As. (2 points)
$M\left(\mathbf{Y}_{\text {c })}=1479.06 \times 0.2818=416.80 \mathrm{~g} \mathrm{~mol}^{-1}\right.$
We know that Y must be from the group 16 in the periodic table, so possible candidates are - $\mathrm{O}, \mathrm{S}, \mathrm{Se}$, Te. $\mathbf{Y}=\mathrm{S}$ (2 points), since we know that the most abundant minerals of arsenic are sulfides - orpiment $\left(\mathrm{As}_{2} \mathrm{~S}_{3}\right)$, realgar $\left(\mathrm{As}_{4} \mathrm{~S}_{4}\right)$ and enargite $\left(\mathrm{Cu}_{3} \mathrm{AsS}_{4}\right)$. Meaning that, $c=13$.
Tennantite $=\mathrm{Cu}_{12} \mathrm{As}_{4} \mathrm{~S}_{13}$ (1 point)
b) i)

A $-\mathrm{As}_{4} \mathrm{~S}_{4}$ (realgar)
B - $\mathrm{As}_{2} \mathrm{O}_{3}$ or $\mathrm{As}_{4} \mathrm{O}_{6}$
C $-\mathrm{AsF}_{3}$
D - $\left[\mathrm{AsF}_{2}{ }^{+}\right]\left[\mathrm{SbF}_{6}{ }^{-}\right]$
E - [ $\left.\mathrm{Cs}^{+}\right]\left[\mathrm{AsF}_{4}{ }^{-}\right]$
F - $\mathrm{AsCl}_{3}$
G-AsH3
K-GaAs
Marking: 2 points for compound $\mathbf{A}, 1$ point for compounds $\boldsymbol{B}-\mathbf{G}, \boldsymbol{K}$.
ii)


H

$$
+2 p
$$



I
$+2 p$


J
$+2 p$
c)

Tennantite $\rightarrow \mathbf{A}: \mathrm{Cu}_{12} \mathrm{As}_{4} \mathrm{~S}_{13} \rightarrow 6 \mathrm{Cu}_{2} \mathrm{~S}+\mathrm{As}_{4} \mathrm{~S}_{4}+3 \mathrm{~S}$
Actually, disulfur $\mathrm{S}_{2}$ is formed under these conditions: $2 \mathrm{Cu}_{12} \mathrm{As}_{4} \mathrm{~S}_{13} \rightarrow 12 \mathrm{Cu}_{2} \mathrm{~S}+2 \mathrm{As}_{4} \mathrm{~S}_{4}+3 \mathrm{~S}_{2}$
$\mathrm{A} \rightarrow \mathrm{B}: \mathrm{As}_{4} \mathrm{~S}_{4}+7 \mathrm{O}_{2} \rightarrow 2 \mathrm{As}_{2} \mathrm{O}_{3}+4 \mathrm{SO}_{2}$
$\mathrm{B} \rightarrow \mathrm{C}: \mathrm{As}_{2} \mathrm{O}_{3}+6 \mathrm{HF} \rightarrow 2 \mathrm{AsF}_{3}+3 \mathrm{H}_{2} \mathrm{O}$
$\mathbf{C} \rightarrow \mathbf{D}: \mathrm{AsF}_{3}+\mathrm{SbF}_{5} \rightarrow\left[\mathrm{AsF}_{2}\right]\left[\mathrm{SbF}_{6}\right]$
$\mathrm{C} \rightarrow \mathrm{E}: \mathrm{AsF}_{3}+\mathrm{CsF} \rightarrow \mathrm{Cs}\left[\mathrm{AsF}_{4}\right]$
$\mathrm{B} \rightarrow \mathrm{F}: \mathrm{As}_{2} \mathrm{O}_{3}+6 \mathrm{HCl} \rightarrow 2 \mathrm{AsCl}_{3}+3 \mathrm{H}_{2} \mathrm{O}$
$\mathbf{F} \rightarrow \mathbf{G}: 4 \mathrm{AsCl}_{3}+3 \mathrm{NaBH}_{4} \rightarrow 4 \mathrm{AsH}_{3}+3 \mathrm{NaCl}+3 \mathrm{BCl}_{3}$
F $\rightarrow \mathbf{J}: \mathrm{AsCl}_{3}+\mathrm{C}_{2} \mathrm{H}_{2} \rightarrow \mathrm{ClCHCHAsCl}_{2}$
$\mathbf{G} \rightarrow \mathbf{K}: \mathrm{AsH}_{3}+\mathrm{Ga}\left(\mathrm{CH}_{3}\right)_{3} \rightarrow \mathrm{GaAs}+3 \mathrm{CH}_{4}$
$\mathbf{B} \rightarrow \mathbf{H}: \mathrm{As}_{2} \mathrm{O}_{3}+4 \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{~K} \rightarrow\left[\left(\mathrm{CH}_{3}\right)_{2} \mathrm{As}\right]_{2} \mathrm{O}+2 \mathrm{~K}_{2} \mathrm{CO}_{3}+2 \mathrm{CO}_{2}$
$\mathrm{H} \rightarrow \mathrm{I}:\left[\left(\mathrm{CH}_{3}\right)_{2} \mathrm{As}\right]_{2} \mathrm{O}+2 \mathrm{HgO}+\mathrm{H}_{2} \mathrm{O} \rightarrow 2\left(\mathrm{CH}_{3}\right)_{2} \mathrm{As}(=\mathrm{O}) \mathrm{OH}+2 \mathrm{Hg}$
Marking: 1 point for every correct reaction ( 0.5 p for correct species, $0.5 p$ for correct coefficients). Give full credit for the first reaction if students provide a correctly balanced equation using $S_{8}$. Full marks are also awarded if $\mathrm{As}_{4} \mathrm{O}_{6}$ is used instead of $\mathrm{As}_{2} \mathrm{O}_{3}$.
d)

BAL

product
$+2 p$
e) $\mathrm{AsF}_{2}{ }^{+}$- bent linear or just bent (1 point), $\mathrm{SbF}_{6}{ }^{-}$- octahedral (1 point)
f)
${ }^{19}$ F NMR: 3 resonances

- quartet (1:1:1:1)
- overlapping sextet (1:1:1:1:1:1) and octet (1:1:1:1:1:1:1:1) in a rough 1.34:1 ratio of intensities
${ }^{75}$ As NMR: 1 resonance - triplet (1:2:1)
${ }^{121}$ Sb NMR: 1 resonance - septet (1:6:15:20:15:6:1)
Marking: 1 point for every correct number of resonances (3 points total), 0.5 points for determining every splitting pattern (2.5 points total) and 0.5 points for every correct ratio of intensities ( 2.5 points total). 0.5 bonus points for calculating the ratio of ${ }^{121} \mathrm{Sb}$ - and ${ }^{123} \mathrm{Sb}$-coupled ${ }^{19} \mathrm{~F}$ signals and another 0.5 bonus points for mentioning the overlap.


## Problem 2. Thermodynamics of electrochemical $\mathrm{CO}_{2}$ capture

1. Using the Nernst equation write an expression for the reduction half-cell potential $E$.

$$
E=E^{0}-R T / m F \ln \left(\left[\mathrm{~A}^{m-}\right] /[\mathrm{A}]\right)-1 p t
$$

2. Write an expression for the equilibrium constant $K$ for the given reaction, assuming the reference pressure $P_{0}$ to be 1 .

$$
K=\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right] /\left(\left[\mathrm{A}^{m}\right] \cdot \mathrm{P}_{\mathrm{CO}_{2}}{ }^{m}\right)-1 p t
$$

3. Find expressions for $f_{1}\left(X_{A^{\prime}}\right)$ and $f_{2}\left(K P_{\mathrm{CO2}^{2}}{ }^{m}\right)$.
```
Starting from \(E=E^{0}-R T / m F \ln \left(\left[\mathrm{~A}^{m-}\right] /[\mathrm{A}]\right)\),
\[
-1 p t
\]
```

let's consider $\left[\mathrm{A}^{m-}\right] /[\mathrm{A}]$ part, while also remembering that:

$$
\begin{align*}
& A_{0}=[\mathrm{A}]+\left[\mathrm{A}^{m-}\right]+\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right]  \tag{1}\\
& x_{\mathrm{A}^{\prime}}=\left(\left[\mathrm{A}^{m-}\right]+\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m}-\right] / A_{0}\right.  \tag{2}\\
& \left.K=\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right] /\left(\left[\mathrm{A}^{m}\right] \cdot\right] \cdot P_{\mathrm{CO}_{2}}^{m}\right) \tag{3}
\end{align*}
$$

From (2): $\quad\left(\left[\mathrm{A}^{m} \cdot\right]+\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right]\right)=x_{A^{\prime}} A_{0}$
Insert in (1): $\quad A_{0}=[\mathrm{A}]+x_{\mathrm{A}}, A_{0}$
Solve for $[A]:[A]=A_{0}\left(1-X_{A}\right) \quad-1 p t$
Also from (2): $A_{0}=\left(\left[\mathrm{A}^{m-}\right]+\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m \cdot}\right]\right) / x_{A^{\prime}}$
So $\quad[\mathrm{A}]=\left(1-x_{A^{\prime}}\right) / x_{A^{\prime}} \cdot\left(\left[\mathrm{A}^{m-}\right]+\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right]\right) \quad-1 p t$
And hence: $\quad\left[\mathrm{A}^{m-}\right] /[\mathrm{A}]=x_{A} /\left(1-x_{A^{\prime}}\right) \cdot\left[\mathrm{A}^{m-}\right] /\left(\left[\mathrm{A}^{m-}\right]+\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right]\right)$
Now in second term divide through $\left[A^{m}\right]$ :

$$
\left[\mathrm{A}^{m-}\right] /[\mathrm{A}]=x_{A} /\left(1-x_{A^{\prime}}\right) \cdot 1 /\left(1+\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right] /\left[\mathrm{A}^{m-}\right]\right)
$$

But from (3): $\left[\mathrm{A}\left(\mathrm{CO}_{2}\right)_{m}^{m-}\right] /\left[\mathrm{A}^{m-}\right]=K \mathrm{CO}_{\mathrm{CO}}{ }^{m} \quad-1 \mathrm{pt}$
And hence: $\quad\left[\mathrm{A}^{m-}\right] /[\mathrm{A}]=x_{A} /\left(1-x_{A}\right) \cdot 1 /\left(1+K P_{\mathrm{CO}_{2}}{ }^{m}\right)$
So we can rewrite equation for $E$ :

$$
\begin{aligned}
& E=E^{0}-R T / m F \ln \left(x_{A} /\left(1-x_{A}\right) \cdot 1 /\left(1+K P_{\operatorname{CO2}}{ }^{m}\right)\right) \\
& E=E^{0}-R T / m F \operatorname{In}\left(x_{A} /\left(1-x_{A}\right)\right)-R T / m F \ln \left(1 /\left(1+K P_{\mathrm{CO}^{2}}{ }^{m}\right)\right) \\
& E=E^{0}+R T / m F \ln \left(\left(1-x_{A}\right) / x_{A}\right)+R T / m F \ln \left(1+K P_{\mathrm{CO}^{2}}{ }^{m}\right)-1 p t
\end{aligned}
$$

And so:

$$
f_{1}\left(x_{A^{\prime}}\right)=\ln \left[\left(1-x_{A^{\prime}}\right) / x_{A^{\prime}}\right]
$$

$$
\mathrm{f}_{2}\left(\boldsymbol{K} \boldsymbol{P}_{\mathrm{CO} 2}\right)=\ln \left(1+K \boldsymbol{P}_{\mathrm{CO} 2}{ }^{m}\right)-1 p t
$$

Overall - 6 pts
4. Write an expression for $E^{\mathrm{dev}}$ in this case.
(In case you could not do the previous question, provide the answer using $f_{1}\left(x_{A^{\prime}}\right)$ and $f_{2}\left(K P_{\mathrm{COO}_{2}}{ }^{m}\right)$ )

$$
\begin{aligned}
& E^{\mathrm{dev}}=R T / m F \cdot f_{2}\left(K P_{\mathrm{CO}_{2}}{ }^{m}\right) \text { or } \\
& E^{\mathrm{dev}}=R T / m F \ln \left(1+K P_{\mathrm{CO}_{2}}{ }^{m}\right)-1 \mathrm{pt}
\end{aligned}
$$

Part II - Thermodynamical analysis (9 pts)
5. Calculate the total $\mathrm{CO}_{2}$ content $x_{\mathrm{CO2}}$ for cases $\alpha=0.25$ and $\alpha=0.75$.

```
x CO2 }=0.25\cdot500\cdot1/(1+500\cdot1)+0.05\cdot1=0.2995-1 pt
x cO2 = 0.75\cdot500\cdot1/(1+500\cdot1)+0.05\cdot1=0.7985-1 pt
```

6. Calculate the partial pressure $P_{\mathrm{CO2}}$ at point C .
(In case you could not calculate $x_{\mathrm{CO2}}$ in the previous question, use a value $x_{\mathrm{CO2}}=0.35$ )
```
0.2995 = 0.75\cdot500\cdotx/(1+500\cdotx)+0.05\cdotx -1 pt
x=0.00133 bar -1 pt
```

For alternative value:
$0.35=0.75 \cdot 500 \cdot x /(1+500 \cdot x)+0.05 \cdot x$
$x=0.00175$ bar
7. Assign all the described steps with points shown in the $E^{\mathrm{dev}}$ vs. a diagram.
(In the form: 1. X to Y )
Four-stage system:
$\begin{array}{ll}\text { 1. A to C } & 0.5 \mathrm{pt} \\ \text { 2. C to D } & 0.5 \mathrm{pt} \\ \text { 3. D to F } & 0.5 \mathrm{pt} \\ \text { 4. F to A } & 0.5 \mathrm{pt}\end{array}$
Two-stage system:
$\begin{array}{ll}\text { 1. } A \text { to } B \text { to } D & 1 \mathrm{pt} \\ \text { 2. } D \text { to } \mathrm{E} \text { to } \mathrm{A} & 1 \mathrm{pt}\end{array}$

The work required to perform the capture-release cycle is described as the area enclosed by the cycle in the $E^{\text {dev }}$ vs. a diagram.
8. Tick the correct answer, consistent with your answer to the previous part.

- Four-stage system requires less work.
$\square$ - Two-stage system requires less work.
1 pt

References:
https://www.sciencedirect.com/science/article/abs/pii/S175058361930427X

1. Assuming that the cubic cell given in Fig. 1 corresponds to the composition of whole material, calculate the x value in empirical formula $\mathrm{Fe}_{\mathrm{x}} \mathrm{Cr}_{1-\mathrm{x}}$.

## Solution:

12 Fe atoms are centered at the edges and one atom - in the center of the cube. Therefore, the count of Fe atoms that reside in the cubic cell is ( 1 point):

$$
12 \cdot \frac{1}{4}+1=4
$$

8 Cr atoms are centered at the vertices, 6 - at the face centers and 8 atoms are inside the cell (at z $=0.25$ and $\mathrm{z}=0.75$ planes). Therefore, the count of Cr atoms that reside in the cubic cell is $(\mathbf{1}$ point):

$$
8 \cdot \frac{1}{8}+6 \cdot \frac{1}{2}+8=12
$$

The ratio is:

$$
\frac{n(\mathrm{Fe})}{n(\mathrm{Cr})}=\frac{4}{12}=\frac{x}{1-x}
$$

Solution of the equation is $x=0.25$ ( 1 point)
2. The lattice parameter of the cell given in Fig. 1 is 576 picometers. Calculate the density of ferrochrome. Express the answer in $\mathrm{g} \cdot \mathrm{cm}^{-3}$ dimensions.

## Solution:

The mass of the cubic cell is (1 point):

$$
m_{\text {cell }}=m_{F e}+m_{C r}=\frac{N_{F e}}{N_{A}} \cdot M(F e)+\frac{N_{C r}}{N_{A}} \cdot M(C r)=\frac{4 M(F e)+12 M(C r)}{N_{A}}
$$

Then the density of ferrochrome, using the assumption that one cell represents overall composition, is equal to (1 point):

$$
\rho_{\text {cell }}=\frac{m_{\text {cel }}}{V_{\text {cell }}}=\frac{4 M(F e)+12 M(C r)}{N_{A}{ }^{3}}
$$

Calculation (1 point):

$$
\rho_{\text {cell }}=\frac{4 \cdot 55.85 \frac{\mathrm{~g}}{\mathrm{~mol}}+12 \cdot 52.00 \frac{\mathrm{~g}}{\mathrm{~mol}}}{6.0221 \cdot 10^{23} \mathrm{~mol}^{-1} \cdot\left(5.76 \cdot 10^{-8} \mathrm{~cm}\right)^{3}}=7.36 \mathrm{~g} \cdot \mathrm{~cm}^{-3}
$$

3. The experimental ferrochrome density value differs by $5 \%$ compared with the result you've calculated in question 2. Which of the following statements can explain such a difference? Circle correct answer letter(s)

| b) | Formation of vacancies in nodes of crystal lattice (1 point) |
| :---: | :--- |
| c) | Because of random distribution of Fe and Cr atoms in the lattice one cubic cell does not <br> ideally correspond to the actual composition of material (1 point) |
| d) | Chemical interactions between Fe and Cr cause the significant change of metallic radii of Fe <br> and Cr atoms (incorrect option, their chemical interactions are very similar to the interaction <br> in pure iron or chromium crystals so we would not expect a significant change of radii) |
| e) | In solid solutions lattice parameter values fluctuates significantly (incorrect option, Fe and <br> Cr atoms have similar radii so lattice parameter remains around the same value) |

4. Write chemical formula of byproduct.

## Answer: MgO (1 point)

Explanation: La atoms can substitute only Mg atoms in forsterite and there is oxygen excess from the $\mathrm{La}_{2} \mathrm{O}_{3}$, that means that byproduct is a material, consisting of magnesium and oxygen.
5. Express index y as a function of x .

## Solution:

Forsterite must remain neutral during the exchange of $\mathrm{Mg}^{2+}$ and $\mathrm{La}^{3+}$ ions. Thus every three $\mathrm{Mg}^{2+}$ ions are substituted by two $\mathrm{La}^{3+}$ ions (condition of electric charge balance) (1 point)

If $x \mathrm{~mol} \mathrm{La}^{3+}$ are introduced into 1 mol of $\mathrm{Mg}_{2} \mathrm{SiO}_{4}$, that means that $\frac{3 x}{2} \mathrm{~mol} \mathrm{Mg}^{2+}$ must be excluded from the material. The total amount of magnesium was 2 mol , therefore ( $\mathbf{1}$ point):

$$
y=2-\frac{3 x}{2}
$$

The empirical formula can be written as $\mathrm{La}_{x} \mathrm{Mg}_{2-1.5 \mathrm{x}} \mathrm{SiO}_{4}$
6. When $\mathrm{La}^{3+}$ ions substitute $\mathrm{Mg}^{2+}$ ions, a certain concentration of vacancies are formed. Vacancies influence electrical conductivity of ionic solid solution. Which electric charge transfer mechanism occurs in $\mathrm{La}_{x} \mathrm{Mg}_{y} \mathrm{SiO}_{4}$ solid solution? Circle one correct answer letter.

| a) | $\mathrm{Mg}^{2+}$ migrates to the vacancy, a new vacancy is formed in $\mathrm{Mg}^{2+}$ node |
| ---: | :--- |
| b) | $\mathrm{La}^{3+}$ migrates to the vacancy, a new vacancy is formed in $\mathrm{La}^{3+}$ node |
| c) | $\mathrm{Si}^{4+}$ migrates to the vacancy, a new vacancy is formed in $\mathrm{Si}^{4+}$ node |
| d) | $\mathrm{O}^{2-}$ migrates to the vacancy, a new vacancy is formed in $\mathrm{O}^{2-}$ node |
| e) | $\mathrm{Mg}^{2+}$ or $\mathrm{La}^{3+}$ migrates to the vacancy, a new vacancy is formed in $\mathrm{Mg}^{2+}$ or $\mathrm{La}^{3+}$ node $(\mathbf{1}$ <br> point) (explanation: $\mathrm{Mg}^{2+}$ and $\mathrm{La}^{3+}$ share the same nodal positions, and $\mathrm{SiO}_{4}^{4-}$ tetrahedral <br> ions both electrostatically and sterically cannot move to cation nodal positions) |
| f) | $\mathrm{Mg}^{2+}, \mathrm{La}^{3+}$ or $\mathrm{Si}^{4+}$ migrates to the vacancy, a new vacancy is formed in $\mathrm{Mg}^{2+}, \mathrm{La}^{3+}$ or $\mathrm{Si}^{4+}$ <br> node |
| g) | $\mathrm{Mg}^{2+}, \mathrm{La}^{3+}, \mathrm{Si}^{4+}$ or $\mathrm{O}^{2-}$ migrates to the vacancy, a new vacancy is formed in $\mathrm{Mg}^{2+}, \mathrm{La}^{3+}, \mathrm{Si}^{4+}$ <br> or $\mathrm{O}^{2-}$ node |

h) Free electrons migrate from vacancy to vacancy
7. By performing electrical conductivity measurements it was calculated that concentration of vacancies in lanthanum-doped forsterite is $6.2 \cdot 10^{17} \mathrm{~cm}^{-3}$. Density of the material is $3.223 \mathrm{~g} \cdot \mathrm{~cm}^{-3}$. One unit cell contains one silicon and four oxygen atoms. Calculate index $x$ in formula $\mathrm{La}_{x} \mathrm{Mg}_{y} \mathrm{SiO}_{4}$ by assuming that all vacancies are formed because of $\mathrm{La}^{3+}-\mathrm{Mg}^{2+}$ exchange.

## Solution:

Because one silicon and four oxygen atoms are in one unit cell, one formula unit belongs to one unit cell. Then the mass of one unit cell is ( $\mathbf{1}$ point):

$$
m_{\text {cell }}=m\left(\operatorname{La}_{x} M g_{y} \mathrm{SiO}_{4}\right)=\frac{N}{N_{A}} \cdot M\left(\mathrm{La}_{x} M g_{y} \mathrm{SiO}_{4}\right)=\frac{M\left(\operatorname{La}_{x} M g_{y} \mathrm{SiO}_{4}\right)}{N_{A}}
$$

Then the volume of unit cell can be calculated from density:

$$
V_{\text {cell }}=\frac{m_{\text {cell }}}{\rho}=\frac{M\left(L_{x} M g_{y} S i O_{4}\right)}{\rho N_{A}}
$$

There is one vacancy per $V=\left(6.2 \cdot 10^{17} \mathrm{~cm}^{-3}\right)^{-1}=1 \cdot 6 \cdot 10^{-18} \mathrm{~cm}^{3}$ volume (1 point). We introduce $N_{\text {cell }}$ - amount of unit cells in volume $V$, and $N_{v a c}-$ a fraction of vacancy per unit cell. Then we can deduce that (1 point):

$$
N_{\text {cell }}=\frac{V}{V_{\text {cell }}} \quad \Rightarrow \quad N_{\text {vac }}=\frac{1}{N_{\text {cell }}}=\frac{V_{\text {cell }}}{V}
$$

We expect a small fraction of vacancies and a small fraction of lanthanum atoms, so we can approximate that $M\left(\mathrm{La}_{x} \mathrm{Mg}_{y} \mathrm{SiO}_{4}\right) \approx M\left(\mathrm{Mg}_{2} \mathrm{SiO}_{4}\right)$ and calculate $N_{v a c}$ (1 point):

$$
N_{v a c} \approx \frac{M\left(M_{2} S O_{4}\right)}{V \rho N_{A}}=\frac{(2 \cdot 24.31+28.09+4 \cdot 16.00) \frac{g}{m o l}}{1.6 \cdot 10^{-18} \mathrm{~cm}^{3} \cdot 3.223 \frac{\mathrm{~g}}{\mathrm{~cm}^{3}} \cdot 6.0221 \cdot 10^{23} \mathrm{~mol}^{-1}}=4.53 \cdot 10^{-5}
$$

When three $\mathrm{Mg}^{2+}$ ions are exchanged by two $\mathrm{La}^{3+}$ ions, one nodal position becomes a vacancy. That means that lanthanum amount in the formula unit is $x=2 N_{v a c}=9.06 \cdot 10^{-5}$ (1 point).
8. Calculate values $a$ and $b$.

## Solution:

We can separate +2 oxidation state and +3 oxidation state iron in the empirical formula like this:

$$
L i_{x} F e_{y}^{I I} F e_{1-x-y}^{I I I} O
$$

And now we apply electric charge neutrality condition - the sum of all amounts (empirical formula indices) and oxidation states must be equal to 0 ( 1 point).

$$
x \cdot(+1)+y \cdot(+2)+(1-x-y) \cdot(+3)+1 \cdot(-2)=0
$$

We can solve for $y$ ( $\mathbf{1}$ point):

$$
x+2 y+3-3 x-3 y-2=0 \quad \Rightarrow \quad y=1-2 x
$$

Then molar amounts $n\left(F e^{3+}\right)$ ir $n\left(F e^{2+}\right)$ are proportional to their indices, so the ratio is (1 point):

$$
r=\frac{n\left(F e^{3+}\right)}{n\left(F e^{2+}\right)}=\frac{1-x-y}{y}=\frac{x}{1-2 x}
$$

We can raise both sides of the equation to the -1 power and extract the reciprocal of x :

$$
\frac{1}{r}=\frac{1-2 x}{x}=\frac{1}{x}-2 \quad \Rightarrow \quad \frac{1}{x}=\frac{1}{r}+2
$$

That shows that $a=1$ and $b=2$ (1 point).
9. Calculate the ratio $r$ and index $x$ from electrochemical measurement data.

## Solution:

If $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4}$ concentration increases, then $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ participates in a reduction to $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4}$ and oxidation process occurs in the reference electrode. It means that we can calculate potential difference by substracting reference electrode potential from reduction process potential (1 point).

$$
\Delta E=E_{\text {reduction }}-E_{\text {reference }}
$$

We know that $E_{\text {reference }}=+0.197 \mathrm{~V}$. Reduction potential can be calculated using Nernst equation (1 point).

$$
E_{\text {reduction }}=E^{\circ}-\frac{R T}{z F} \ln \ln \frac{\left[\mathrm{Fe}(\mathrm{CN})_{6}{ }^{4-}\right]}{\left[\mathrm{Fe}(\mathrm{CN})_{6}{ }^{3-}\right]}=E^{\circ}-\frac{R T}{F} \ln \ln \frac{\left[\mathrm{Fe}(\mathrm{CN})_{6}{ }^{4-}\right]}{\left[\mathrm{Fe}(\mathrm{CN})_{6}{ }^{3-}\right]}
$$

$\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4}$ concentration represents the amount of $\mathrm{Fe}^{2+}$ in the analyzed material and $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ represents the amount of $\mathrm{Fe}^{3+}$ in the analyzed material. That implies (1 point).

$$
E_{\text {reduction }}=E^{\circ}-\frac{R T}{F} \ln \ln \frac{n\left(F e^{2+}\right)}{n\left(F e^{3+}\right)}=E^{\circ}-\frac{R T}{F} \ln \ln \frac{1}{r}=E^{\circ}+\frac{R T}{F} \ln \ln r
$$

Now we can derive $r$ ( $\mathbf{1}$ point):

$$
\begin{gathered}
\frac{R T}{F} \ln \ln r=E_{\text {reduction }}-E^{\circ}=\Delta E+E_{\text {reference }}-E^{\circ} \\
r=\exp \exp \left(\frac{F}{R T} \bullet\left(\Delta E+E_{\text {reference }}-E^{\circ}\right)\right)
\end{gathered}
$$

Calculation (1 point):

$$
r=\exp \exp \left(\frac{96485.3 \frac{\mathrm{C}}{\mathrm{~mol}}}{8.3145 \frac{J}{\mathrm{~K} m \mathrm{~mol}} 298 \mathrm{~K}} \cdot(0.092 \mathrm{~V}+0.197 \mathrm{~V}-0.370 \mathrm{~V})\right)=0.0427
$$

And using the relationship derived in question 8 we can calculate $x$ value ( $\mathbf{1}$ point):

$$
x=\left(\frac{1}{r}+2\right)^{-1}=\left(\frac{1}{0.0427}+2\right)^{-1}=0.0393
$$

10. Show that for orthorhombic lattice with different unit cell lengths $a, b, c$ phosphorescence intensity can be calculated using formula below.

$$
I=\frac{9 \cdot C N \cdot k_{p h}}{9 \cdot k_{p h} \cdot r_{0}^{2}+k_{v i b} \cdot C N^{2} \cdot\left(a^{2}+b^{2}+c^{2}\right)}
$$

## Solution:

No matter which node we select, the first coordination shell comprises of six nodal positions: two at distance $a$, two at distance $b$ and two at distance $c$ from the selected molecule (figure in the right) (1 point).

Maximum possible CN value is 6 . But in solid solutions $C N<6$ (not every nodal position is occupied by A molecule). But because probability to occupy site at distance $a$, or distance $b$, or distance $c$, is exactly $1 / 3$, we can deduce ( 1 point):

$$
C N_{a}=C N_{b}=C N_{b}=\frac{C N}{3}
$$

Now we expand the sum in the denominator of the model equation into three parts (1 point):


$$
I=\frac{C N \cdot k_{p h}}{k_{p h} \cdot r_{0}^{2}+k_{v i b}\left(C N_{a}^{2} \cdot a^{2}+C N_{b}^{2} \cdot b^{2}+C N_{c}^{2} \cdot c^{2}\right)}
$$

We change $C N_{a}, C N_{b}$ and $C N_{c}$ values to $C N$ and derive the final expression (1 point):

$$
\begin{gathered}
I=\frac{C N \cdot k_{p h}}{k_{p h} \cdot r_{0}^{2}+k_{v i b}\left(C N^{2}\right.} 9 \cdot a^{2}+\frac{\left.C N^{2} \cdot b^{2}+\frac{C N^{2}}{9} \cdot c^{2}\right)}{9} \\
I=\frac{C N \cdot k_{p h}}{k_{p h} \cdot r_{0}^{2}+\frac{1}{9} k_{v i b} \cdot c N^{2}\left(a^{2}+b^{2}+c^{2}\right)}=\frac{9 \cdot C N \cdot k_{p h}}{9 \cdot k_{p h} \cdot r_{0}^{2}+k_{v i b} \cdot \bullet N^{2}\left(a^{2}+b^{2}+c^{2}\right)}
\end{gathered}
$$

11. Solid solution $\mathbf{X}$ is prepared by co-crystallising $\mathbf{A}$ and $\mathbf{B}$ in ratio $n(A): n(B)=1: 1$. Solid solution $\mathbf{Y}$ is prepared by co-crystallising $\mathbf{A}$ and $\mathbf{B}$ in ratio $n(A): n(B)=2: 1$. $\mathbf{X}$ phosphoresce 1.25 times more intensely than $\mathbf{Y}$. Calculate the length of the diagonal of orthorhombic unit cell, if $\frac{k_{p h}}{k_{v i b}} \approx 10^{-4}$ and $r_{0} \approx 710 \AA$.

## Solution:

In solid solution $\mathbf{X}, 50 \%$ of nodal positions are occupied by molecules A. Therefore, in average coordination number of A molecules around A molecule is $C N_{X}=0.50 \cdot 6=3$ (1 point).

Similarly, in solid solution $\mathbf{Y}, 2 / 3=66.7 \%$ of nodal positions are occupied by molecules A. That implies $C N_{Y}=2 / 3 \cdot 6=4$ (1 point).

By Pythagorean theorem, diagonal length of the unit cell $d$ can be expressed as ( $\mathbf{1}$ point):

$$
d^{2}=a^{2}+b^{2}+c^{2}
$$

Now we know that (1 point):

$$
\frac{I_{X}}{I_{Y}}=\frac{\frac{9 \cdot C N_{X} \bullet k_{p h}}{9 \cdot k_{p h} \bullet r_{0}^{2}+k_{v i b} \bullet C N_{X}^{2}\left(a^{2}+b^{2}+c^{2}\right)}}{\frac{9 \cdot C N_{Y} \bullet k_{p h}}{9 \cdot k_{p h} \bullet r_{0}^{2}+k_{v i b} \bullet C N_{Y}^{2}\left(a^{2}+b^{2}+c^{2}\right)}}=\frac{\frac{3}{9 \cdot k_{p h} \bullet r_{0}^{2}+k_{v i b} \cdot 9 d^{2}}}{\frac{4}{9 \cdot k_{p h} \bullet r_{0}^{2}+k_{v i b} \cdot 16 d^{2}}}=1.25
$$

We can derive $d$ from the ratio above and calculate its value ( $\mathbf{2}$ points):

$$
\begin{gathered}
9 \cdot k_{p h} \cdot r_{0}^{2}+k_{v i b} \cdot 16 d^{2}=1.25 \cdot \frac{4}{3} \cdot\left(9 \cdot k_{p h} \cdot r_{0}^{2}+k_{v i b} \cdot 9 d^{2}\right) \\
9 \cdot k_{p h} \cdot r_{0}^{2}+k_{v i b} \cdot 16 d^{2}=15 \cdot k_{p h} \cdot r_{0}^{2}+k_{v i b} \cdot 15 d^{2} \\
k_{v i b} d^{2}=6 \cdot k_{p h} \cdot r_{0}^{2} \\
d=r_{0} \sqrt{6 \cdot \frac{k_{p h}}{k_{v i b}}}=710 \AA \sqrt{6 \cdot 10^{-4}}=17.4 \AA
\end{gathered}
$$

Total: $\mathbf{3 7}$ points.

## Problem 4. Kinetics

9 points

1. 2. Select ALL appropriate mechanisms which are consistent with the assumption given in $\mathbf{1}$.

Mechanism (a)
Mechanism (b)
Mechanism (c)
Mechanism (d)
1 point for each correct answer
-1 point for each incorrect answer
No negative points in total
2 points in total for 1. 1.

1. 2. Select ALL graphs that could depict the relationship between $[B]$ and both $t$, time, or $r$, rate of reaction ( 0 ), and are consistent with the condition given in $\mathbf{1}$. Assume a constant state for $[A]$.

Graph (a)
Graph (b)
Graph (c)

1 point for each correct answer
-1 point for each incorrect answer
No negative points in total
3 points in total for 1. 2.
2. For each condition listed below, determine whether the rate-limiting step of the mechanism presented above is step (1), step (2) or neither. Assume that $[A]$ and $[B]$ are much greater than $[A B]$ and $\left[A B_{2}\right]$.
2.1. $k_{1} \gg k_{-1} ; k_{2} \gg k_{1}$
2. 2. $k_{1} \gg k_{-1} ; k_{2} \ll k_{1}$
2.3. $k_{1} \gg k_{-1} ; k_{2} \cong k_{1}$
2.4. $k_{1} \cong k_{-1} ; k_{2} \ll k_{1}$

Condition 2. 1. $\quad \operatorname{Step}(1) \boxtimes$
Condition 2.2. $\quad$ Step (1) $\square$
Condition 2.3. Step (1) $\qquad$
Condition 2.4. $\quad$ Step (1) $\qquad$

Step (2)
Step (2) $\boxtimes$
Step (2)
$\boldsymbol{S t e p}(2) \boxtimes$

Neither
Neither $\square$
Neither $\boxtimes$
Neither $\square$

1 point for each correct answer
0 points for each incorrect answer

4 points total for 2.
3. At time $t=t_{1}$, the concentration of intermediate $A B$ has become constant, i.e. $[A B]=[A B]_{\text {const }}$, and the concentration of reagent $A$ has reached a certain value, ie. $[A]=[A]_{1}$.
3.1. Express the ratio of the rate constants, namely $\frac{k_{1}}{k_{2}}$, using terms $[A]_{1}$ and $[A B]_{\text {const }}$. Assume that $k_{1}, k_{2} \gg k_{-1}$.

The rate of production of $A B_{2}$ can be expressed as follows:

$$
\frac{d\left[A B_{2}\right]}{d t}=k_{2}[B][A B]
$$

Since $[A B]$ is given to be constant, we can assume a steady-state for this compound:

$$
\begin{gathered}
\frac{d[A B]}{d t}=k_{1}[A][B]-k_{-1}[A B]-k_{2}[A B][B]=0 \\
{[A B]=\frac{k_{1}[A][B]}{k_{-1}+k_{2}[B]}}
\end{gathered}
$$

Taking into account that $k_{1}, k_{2} \gg k_{-1}$, we can simplify the equation above as follows:

$$
[A B]=\frac{k_{1}[A][B]}{k_{-1}+k_{2}[B]} \cong \frac{k_{1}[A][B]}{k_{2}[B]}=\frac{k_{1}[A]}{k_{2}}
$$

Using this expression of $[A B]$, we can express the rate of reaction (2) as follows:

$$
\begin{gathered}
\frac{d\left[A B_{2}\right]}{d t}=k_{2}[B][A B]=\frac{k_{1} k_{2}[A][B]}{k_{2}}=k_{1}[A][B] \\
k_{1}[A][B]=k_{2}[B][A B] \Rightarrow \frac{k_{1}}{k_{2}}=\frac{[A B]}{[A]}
\end{gathered}
$$

At time $t=t_{1}$ :

$$
\frac{k_{1}}{k_{2}}=\frac{[A B]_{\text {cons }}}{[A]_{1}}
$$

1 point for showing $\frac{d\left[A B_{2}\right]}{d t}=k_{2}[B][A B]$
2 points for correctly applying the steady-state intermediate law for $[A B]$
1 point for simplifying the initial expression of $[A B]$
2 points for deriving the equality $k_{1}[A][B]=k_{2}[B][A B]$
1 point for finding the ratio of the rate constants

7 points in total for 3.1.
4.
4. 1. Assuming that under given conditions steps (1) and (2) proceed much slower than step (3), show that the observed rate constant, $k_{\text {obs }}$, is approximately equal to rate constant $k_{1}$.

$$
\frac{d[A B C]}{d t}=k_{3}[C][A B]
$$

Assuming the steady-state intermediate law for compound $A B$ :

$$
\begin{gathered}
\frac{d[A B]}{d t}=k_{1}[A][B]-k_{-1}[A B]-k_{2}[A B][B]-k_{3}[A B][C]=0 \\
{[A B]=\frac{k_{1}[A][B]}{k_{-1}+k_{2}[B]+k_{3}[C]}}
\end{gathered}
$$

Given that step (2) proceeds much slower than step (3), their reaction rates can be compared as follows:

$$
\begin{aligned}
k_{2}[A B][B] & \ll k_{3}[C][A B] \\
k_{2}[B] & \ll k_{3}[C]
\end{aligned}
$$

We can therefore simplify the expression of $[A B]$ :

$$
[A B]=\frac{k_{1}[A][B]}{k_{-1}+k_{2}[B]+k_{3}[C]} \cong \frac{k_{1}[A][B]}{k_{3}[C]}
$$

Thus, the rate of production of $[A B C]$ becomes:

$$
\frac{d[A B C]}{d t}=k_{3}[C] \frac{k_{1}[A][B]}{k_{3}[C]}=k_{1}[A][B]
$$

Therefore $k_{o b s} \cong k_{1}$.

1 point for showing $\frac{d[A B C]}{d t}=k_{3}[C][A B]$
2 points for correctly applying the steady-state intermediate law for $[A B]$
3 points for simplifying the initial expression of $[A B]$
1 point for obtaining $k_{o b s} \cong k_{1}$

7 points total for 4.1.
4. 2. Using signs $>,<$ and/or $\cong$, denote the relationship between reactions' (2) and (3) Arrhenius pre-factors, $A_{2}$ and $A_{3}$, and activation energies, $E_{a 2}$ and $E_{a 3}$, respectively. Assume that Arrhenius pre-factors and activation energies of these reactions are independent of temperature.

At lower temperature, $k_{2}<k_{3} \Rightarrow A_{2} \cdot \exp \left(\frac{-E_{a 2}}{R T}\right)<A_{3} \cdot \exp \left(\frac{-E_{a 3}}{R T}\right)$
As the temperature increases, $k_{2}$ increases at a faster rate than $k_{3}$, meaning $\frac{E_{a 2}}{T}$ decreases at a faster rate than $\frac{E_{a 3}}{T}$. Therefore $E_{a 2}>E_{a 3}$ and $\exp \left(\frac{-E_{a 2}}{R T}\right)<\exp \left(\frac{-E_{a 3}}{R T}\right)$. If $k_{2}=k_{3}$ and $\exp \left(\frac{-E_{a 3}}{R T}\right)<\exp \left(\frac{-E_{a 4}}{R T}\right)$, then the following must be true: $A_{2}>A_{3}$.

$$
A_{2}>A_{3}
$$

$$
E_{a 2}>E_{a 3}
$$

0 points if both notations are incorrect
3 points if one of the notations is correct
8 points if both notations are correct

8 points in total
5. Certain amounts of $B, C$ and $A B$ were added to a container under conditions that favor only reactions (2) and (3). Assume, that the initial concentration of $A B,[A B]_{0}$, is much greater than initial concentrations of both $B,[B]_{0}$, and $C,[C]_{0}$.

At time $t=t_{3}$, concentrations of compounds $A B_{2}$ and $A B C$ were measured and their values were found to be equal.
5.1. Express the ratio of initial concentrations of $B$ and $C$, namely $\frac{[B]_{0}}{[C]_{0}}$, in terms of $[A B]_{0}, k_{2}, k_{3}$ and $t_{3}$.

Concentrations of compounds $A B_{2}$ and $A B C$ at time $t=t_{3}$ can be expressed as follows:
$\left[A B_{2}\right]=[B]_{0}-[B]_{t}$
$[A B C]=[C]_{0}-[C]_{t}$,
where $[B]_{t}$ and $[C]_{t}$ are concentrations of their respective compounds at time $t=t_{3}$.
Given that $[A B] \gg[B],[C]$, we can assume $[A B]$ stays constant throughout the remainder of the reaction and can be denoted as $[A B]_{0}$.

$$
\begin{align*}
& \frac{d[B]}{d t}=-k_{2}[A B][B]=-k_{2}[A B]_{0}[B] \Rightarrow[B]_{t}=[B]_{0} \cdot \exp \left(-k_{2}[A B]_{0} t{ }_{3}\right)  \tag{7}\\
& \frac{d[C]}{d t}=-k_{3}[A B][C]=-k_{2}[A B]_{0}[C] \Rightarrow[C]_{t}=[C]_{0} \cdot \exp \left(-k_{3}[A B]_{0} t_{3}\right) \tag{8}
\end{align*}
$$

Plugging in these values into (5) and (6), we obtain:
$\left[A B_{2}\right]=[B]_{0} \cdot\left(1-\exp \left(-k_{2}[A B]_{0} t_{3}\right)\right)$

$$
[A B C]=[C]_{0} \cdot\left(1-\exp \left(k_{3}[A B]_{0} t_{3}\right)\right)
$$

Given that $\left[A B_{2}\right]$ and $[A B C]$ are equal, we derive the following equation:
$[B]_{0} \bullet\left(1-\exp \left(-k_{2}[A B]_{0} t_{3}\right)\right)=[C]_{0} \bullet\left(1-\exp \left(k_{3}[A B]_{0} t_{3}\right)\right)$

$$
\frac{[B]_{0}}{[C]_{0}}=\frac{1-\exp \left(-k_{3}[A B]_{0} t_{3}\right)}{1-\exp \left(-k_{2}[A B]_{0} t{ }_{3}\right)}
$$

1 points each for obtaining (5) and (6)
2 points each for obtaining (7) and (8)
2 points for deriving equation (9)
1 point for finding the ratio of initial concentrations

## 9 points in total for 5.1.

5.2. Calculate the ratio of the rates of reactions (2) and (3), namely $\frac{r_{2}}{r_{3}}$, at time $t=t_{3}$, when $[A B]_{0}=1.20 \cdot 10^{-3} \mathrm{~mol} \cdot \mathrm{~L}^{-1}, \quad k_{2}=1.40 \cdot 10^{-3} \mathrm{~L} \cdot \mathrm{~mol}^{-1} \cdot \mathrm{~s}^{-1}, \quad k_{3}=5.60 \cdot 10^{-4} \mathrm{~L} \cdot \mathrm{~mol}^{-1} \cdot \mathrm{~s}^{-1}$ and $t_{3}=2.50 \cdot 10^{3} \mathrm{~s}$.

At time $t=t_{3}$ :

$$
\frac{r_{2}}{r_{3}}=\frac{k_{2}[B]_{t}[A B]}{k_{3}[C]_{t}[A B]}=\frac{k_{2}[B]_{t}}{k_{3}[C]_{t}}
$$

Plugging in values from (7) and (8) we obtain:

$$
\frac{r_{2}}{r_{3}}=\frac{k_{2}[B]_{0} \cdot \exp \left(-k_{2}[A B]_{0} t_{3}\right)}{k_{3}[C]_{0} \cdot \exp \left(-k_{3}[A B]_{0} t_{3}\right)}=\frac{k_{2}}{k_{3}} \bullet \frac{[B]_{0}}{[C]_{0}} \bullet \frac{\exp \left(-k_{2}[A B]_{0} t_{3}\right)}{\exp \left(-k_{3}[A B]_{0} t_{3}\right)}
$$

Using the derived expression of $\frac{[B]_{0}}{[C]_{0}}$ in 5.1.:

$$
\frac{r_{2}}{r_{3}}=\frac{k_{2}}{k_{3}} \cdot \frac{1-\exp \left(-k_{3}[A B]_{0} t_{3}\right)}{1-\exp \left(-k_{2}[A B]_{0} t{ }_{3}\right)} \cdot \frac{\exp \left(-k_{2}[A B]_{0} t_{3}\right)}{\exp \left(-k_{3}[A B]_{0} t_{3}\right)}
$$

Using values given in 5.2. we obtain a numerical expression of $\frac{r_{3}}{r_{4}}$ :
$\frac{r_{2}}{r_{3}}=\frac{1.40 \cdot 10^{-3} s^{-1} \cdot \exp \left(-1.40 \cdot 10^{-3} \mathrm{~s}^{-1} \cdot 1.20 \cdot 10^{-3} \mathrm{~mol} \cdot \mathrm{~L}^{-1} \cdot 2.50 \cdot 10^{3} \mathrm{~s}\right)\left(1-\exp \left(-5.60 \cdot 10^{-4} \mathrm{~s}^{-1} \cdot 1.20 \cdot 10^{-3} \mathrm{~mol} \cdot \mathrm{~L}^{-1} \cdot 2.50 \cdot 10^{3} \mathrm{~s}\right)\right)}{5.60 \cdot 10^{-4} \mathrm{~s}^{-1} \cdot \exp \left(-5.60 \cdot 10^{-4} \mathrm{~s}^{-1} \cdot 1.20 \cdot 10^{-3} \mathrm{~mol} \cdot \mathrm{~L}^{-1} \cdot 2.50 \cdot 10^{3} \mathrm{~s}\right)\left(1-\exp \left(-1.40 \cdot 10^{-3} \mathrm{~s}^{-1} \cdot 1.20 \cdot 10^{-3} \mathrm{~mol} \cdot \mathrm{~L}^{-1} \cdot 2.50 \cdot 10^{3} \mathrm{~s}\right)\right)}$ $\frac{r_{2}}{r_{3}}=0.9987$
2 points for showing $\frac{r_{2}}{r_{3}}=\frac{k_{2}[B]_{t}}{k_{3}[C]_{t}}$
2 points for using the answer obtained in 5.1.
2 points for obtaining the correct numerical expression of $\frac{r_{2}}{r_{3}}$
6 points in total for 5.2.
46 points in total

Problem 5. Total synthesis of (-)-Colombiasin A
References:

- https://onlinelibrary.wiley.com/doi/epdf/10.1002/anie.200601872?saml_referrer
- https://onlinelibrary.wiley.com/doi/epdf/10.1002/ange. 200462268
- https://pubmed.ncbi.nlm.nih.gov/11822436/
- Squarate X spectroscopic data - suppmat, article

1) 



A
+2 p


B
+2 p


C
+1p


D
+2 $p$


E
+2 p

One-time penalty of -1 p for every incorrect assignment of stereochemistry, including geometry about the double bond in $\mathbf{E}$.
2) DMSO (best for solvating $\mathrm{Na}^{+}$) (2 points)
3) The reaction mechanism is that of the Julia-Kocienski olefination, a refined version of the well-known Julia olefination. The aldehyde is abbreviated as RCHO for the sake of clarity.

4) Assuming the relevant ${ }^{1} \mathrm{H}$ NMR resonances do not overlap significantly with other resonances, the ratio of $E / Z$ isomers can be qualitatively approximated by the ratio of integrals of corresponding ${ }^{1} \mathrm{H}$ resonances (1 point). The alkene protons of $E-E$ and $Z-E$ can be distinguished based on the values of ${ }^{3} J_{H-H}$ coupling constants (1 point). While cis-alkene protons usually have a ${ }^{3} J_{H-H}$ value in the range $7-12$

Hz , the coupling constants of trans-alkene protons usually come in the range $12-18 \mathrm{~Hz}$ ( 1 point even if it has been simply stated that generally ${ }^{3} J_{\mathrm{H}-\mathrm{H}, \mathrm{cis}}<{ }^{3} \mathrm{~J}_{\mathrm{H}-\mathrm{H}, \text { trans }}$ ).
5) $\mathrm{CO}, \mathrm{CO}_{2}, \mathrm{Me}_{2} \mathrm{~S}$ and $\mathrm{Et}_{3} \mathrm{NHCl}$. ( 4 x 0.5 points, HCl accepted in place of ammonium salt)
6)

F
+1 p

G
$+2 p$

X
+2 p

H
+3p

Marking: no marks for writing the chemical formula of $\boldsymbol{X}\left(\mathrm{C}_{9} \mathrm{H}_{12} \mathrm{O}_{3}\right)$.
7)


## Problem 6. Chiral Pool

1.Determine the structures of compounds $\mathbf{B}-\mathbf{D}, \mathbf{F}-\mathbf{H}$. (15 points)

| B | F |
| :---: | :---: |
|  <br> $2 \quad$ points for skeleton/regioselectivity +0.5 points for trans $\mathrm{OH} / \mathrm{Cl}+0.5$ points for correct diastereomer |  <br> 2 points for correct structure 1 point if reduced till aldehyde |
| C | G |
|  <br> 2 points for correct structure <br> 1 point if ketone was protected (through enol form instead of alcohol) |  <br> 2 points for correct structure 1 point if only one of the alcohols were oxidized |
| D | H |
|  <br> 2 points for correct |  |
| skeleton/regioselectivity <br> +1 point for ester and methyl trans | $2 \quad$ points for correct skeleton/regioselectivity +0.5 points for trans OH/lactone + 0.5 points for correct diastereomer |

The reagent $\mathbf{X}$ could be obtained in many ways. In the scheme below, two of the most popular routes are shown.

${ }^{1} \mathrm{H}$ NMR spectra of X2: $6.08(\mathrm{t}, \mathrm{J}=3 \mathrm{~Hz}, 1 \mathrm{H}), 5.63(\mathrm{t}, \mathrm{J}=3 \mathrm{~Hz}, 1 \mathrm{H}), 4.30(\mathrm{t}, \mathrm{J}=7 \mathrm{~Hz}, 2 \mathrm{H}), 2.97$ ( $\mathrm{m}, 2 \mathrm{H}$ ).
2.Determine the structures of compounds X1, X2 and X3. (6 points)


3.Propose a mechanism for the synthesis of X1. (3 points)

4.Propose a reagent(-s) to obtain $\mathbf{X}$ from $\mathbf{X 1}$ in one step. (2 points)

## HBr (2 points)

1 point if proposed reagent can 1) remove TBS or 2) substitute OH to Br
The endgame of the synthesis was planned through a Swern oxidation followed by cyclization to obtain the 8-epigosheimin (K). During the oxidation, an isomer J1 was formed instead of the necessary J2. Although the endgame was quite short, in order to prove the absolute configuration, a different route was taken (through L).



Note, that Ti(IV) salts are strong, oxophilic Lewis acids.
5.Determine the structures of compounds $\mathbf{~ J 1 , ~ L} \mathbf{-} \mathbf{0}$. (10 points)

| J 1 | $\mathbf{N}$ |
| :--- | :--- |


|  <br> 2 points for correct structure 1 point if epimerized any one of carbonyl's alpha positions |  <br> 2 points for correct structure |
| :---: | :---: |
| L <br> 2 points for correct structure (stereochemistry on new center not important) | [0] <br> 2 points for correct structure 1 point if diol/epoxide formed instead |
| [M] <br> 2 points for correct structure | Space for corrections |

6.Choose (from the set of conditions below) the appropriate conditions for the transformation of $\mathbf{J} 2$ to $\mathbf{K}$. (2 points)
nBuLi, diethylamine
$\mathrm{MgSO}_{4}$, toluene, reflux
$\mathrm{BF}_{3} \cdot \mathrm{Et}_{2} \mathrm{O}$
$\mathrm{NaOH}, \mathrm{H}_{2} \mathrm{O}_{2}$
$\mathrm{NaClO} 2, \mathrm{NaH}_{2} \mathrm{PO}_{4}, \mathrm{tBuOH} / \mathrm{H}_{2} \mathrm{O}$
2 points for correct one (minus 1 point for every additional conditions chosen)

